

Solution to Test 1

Q1: $F = kQ^2 / a^2 = 10^{11} Q^2$, $F_{tot} = \sqrt{2} \times 10^{11} Q^2$
 $F_{tot} = 0.1414 Q^2(\mu c) = 14.2, 31.8, 56.6, 88.4 N$

Q2: $V = \sum_i \frac{kQ_i}{r_i} = 9 \times 10^9 \frac{Q(nc) \times 10^{-9}}{0.3} \left(-1 + \frac{2}{\sqrt{2}} \right) = 12.426 Q(nc)$
 $= 124.3, 186.4, 248.5, 310.6V$

Q3: $eV = \frac{1}{2}mv^2 \therefore v = [0.3516 \times 10^{12} V]^{1/2} = 1.18 \times 10^7 m/s, 1.77 \times 10^7 m/s,$
 $2.37 \times 10^7 m/s, 2.96 \times 10^7 m/s.$

Q4: $\lambda = 2\pi a\sigma$, $E = \frac{2k\lambda}{r} = \frac{200}{r} = 200, 250, 400, 500 N/C$

Q5: $C_{eq} = \left\{ c \text{ (ser)} \left[15\mu F \text{ (par)} \left(\underbrace{10\mu F \text{ (ser)} 10\mu F}_{5\mu F} \right) \right] \right\} = \frac{20c}{20+c} = 4, 7.5, 10, 15\mu F.$

Q6: $Q_1 = c_1 \times 10 = 20\mu C$, $Q_2 = 10c_2$, $Q_{net} = 10c_2 - 20\mu$

$$\left. \begin{array}{l} 10c_2 - 20\mu = Q'_1 + Q'_2 \\ \frac{Q'_1}{2\mu} = \frac{Q'_2}{c_2} \end{array} \right\} Q'_1 = 6.66, 10, 12, 13.33\mu C$$

Problem 1: $E_\rho = k \int_b^\infty \frac{\lambda dy}{y^2} = \frac{k\lambda}{b}$ or $E_\rho = k \int_0^\infty \frac{\lambda dy}{(b+y)^2} = \frac{k\lambda}{b}$

Problem 2:

I 1. $E_1 = k2Q / r^2$

2. $E_2 = 0$

3. $E_3 = 0$ ($q_{encl} = 0$)

II $V_p = V_{p\infty} = \int_a^\infty E dr = \int_a^b E_1 dr + \int_b^c E_2 dr + \int_b^c E_3 dr = 2kQ \left(\frac{1}{a} - \frac{1}{b} \right)$

III $V = V_p = 2kQ \left(\frac{b-a}{ab} \right) \therefore C = \frac{2Q}{V} = \frac{ab}{k(b-a)}$
