

UNIVERSITY OF BAHRAIN  
COLLEGE OF SCIENCE  
PHYSICS DEPARTMENT

PHYCS 102  
TEST 3

DATE: 2/1/2001

TIME: 55 MIN.

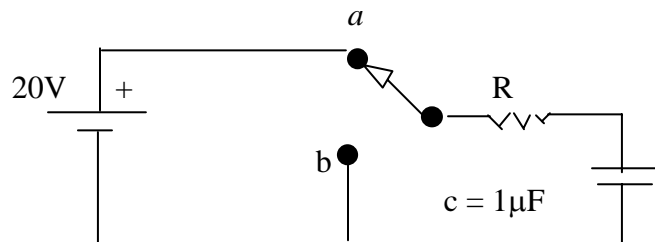
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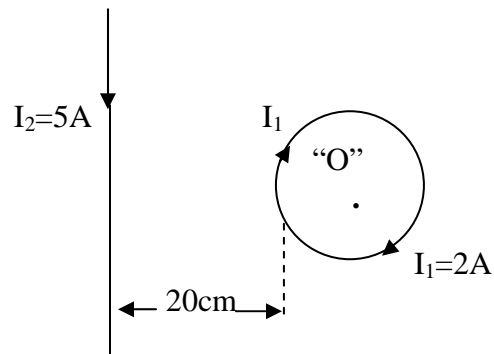
**Q1.** In the circuit shown the capacitor is fully charged. Then, at  $t = 0$  the switch is thrown from "a" to "b". This causes the current to decrease to 0.5 of its initial value in  $40 \mu\text{s}$ .

- Calculate the value of  $R$ .
- What is the value of the capacitor charge  $Q$  at  $t = 0$ ?
- What is the value of  $Q$  at  $t = 60 \mu\text{s}$ ?



$$\begin{aligned} \text{a) } I &= I_0 e^{-t/RC}, 0.5I_0 = I_0 e^{-\frac{40\mu}{R(1\mu)}} \Rightarrow R = 57.7\Omega \\ \text{b) } Q_0 &= c\varepsilon = 20 \mu\text{c} \\ \text{c) } Q &= Q_0 e^{-t/RC} = 20 e^{-\frac{60\mu}{57.7 \times (1\mu)}} = 7.1 \mu\text{c} \end{aligned}$$

**Q2.** In the figure shown below, a circular loop of radius  $R = 20\text{cm}$  carries a current  $I_1 = 2\text{A}$  and a very long straight wire carries a current  $I_2 = 5\text{A}$ . Use superposition method to determine the magnitude and direction of the total magnetic field at the center "O" of the loop.



$$\begin{aligned} B_1 &= \frac{\mu_0 I_1}{2R} = 6.28 \times 10^{-6} T \otimes, B_2 = \frac{\mu_0 I_2}{2\pi r} = \frac{M_0 I_2}{2\pi(0.4)} = 2.5 \times 10^{-6} T \odot \\ B &= B_1 - B_2 = 3.78 \text{ mT } \otimes \end{aligned}$$

**Q3.** A proton is accelerated by 56KV, enters a uniform magnetic field ( $\vec{B}$ ) in a direction perpendicular to ( $\vec{B}$ ). The proton moves in a circular path of radius 8m. Determine:

- a) the magnitude of  $\vec{B}$ ,  
 b) the time required to make 5 revolutions.

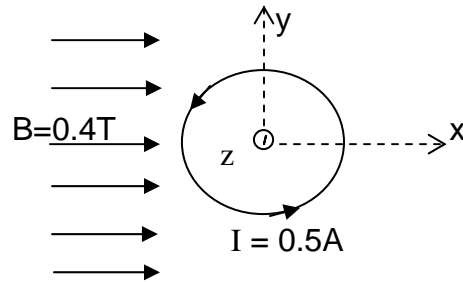
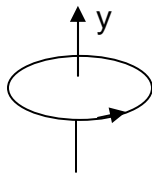
$$\text{a) } eV = \frac{1}{2} m_p v^2, v = \left[ \frac{2 \times 1.6 \times 10^{-19} \times 56 \times 10^3}{1.67 \times 10^{-27}} \right]^{1/2} = 3.276 \times 10^6 \text{ m/s}$$

$$R = mv / qB, \quad 8 = \frac{1.67 \times 10^{-27} \times 3.276 \times 10^6}{1.6 \times 10^{-19} B} \therefore B = 4.274 \text{ mT.}$$

$$\text{b) } T = \frac{2\pi m}{qB} = 1.534 \times 10^{-5} \text{ s}, \quad t = 5T = 7.67 \times 10^{-5} \text{ s.}$$

**Q4.** A circular loop of radius R = 10 cm consists of 50 closely wrapped turns in which each carries a current of 0.5A. The loop is placed in a uniform magnetic field of B = 0.4T directed in the positive x-axis, as shown in the figure.

- a) What is the resultant magnetic force on the loop?  
 b) Calculate the magnitude of the torque  $\vec{\tau}$  on the loop.  
 c) What is the direction of  $\vec{\tau}$ ? Describe the expected rotation of the loop?



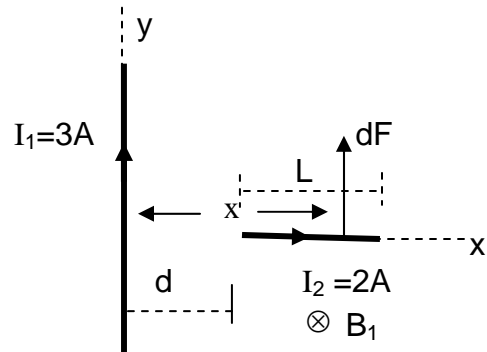
The rotation is around y-axis

$$\text{a) } \sum \vec{F} = 0$$

$$\text{b) } \vec{\tau} = \vec{\mu} \wedge \vec{B} = NI\vec{A} \wedge \vec{B}, \tau = NIAB = 50(0.5)(\pi \times 0.1^2)(0.4) = 0.314 \text{ N.m}$$

$$\text{c) } \vec{\mu} = \mu\vec{k}, \vec{B} = B\vec{i} \therefore \vec{\tau} = \tau \vec{j} \text{ (i.e. in positive y-direction)}$$

- Q5.** A short straight wire of length  $L=0.3\text{m}$  carries a current  $I_2 = 2\text{A}$  is placed perpendicular at a distance  $d= 0.1\text{m}$  near a long straight wire that carries a current  $I_1 = 3\text{A}$  as shown in the figure. Determine the magnitude and direction of magnetic force that exerted on the short wire.



$$dF = I_2 dx \quad B_1 = \frac{\mu_0 I_1}{2\pi x} dx$$

$$F = \frac{\mu_0 I_1 I_2}{2\pi} \int_{0.1}^{0.4} \frac{dx}{x} = 1.66 \mu\text{N} \quad \text{in } y\text{-direction}$$

$$m_p = 1.67 \times 10^{-27} \text{Kg.}$$

$$E = 1.6 \times 10^{-19} \text{C}$$

**Good luck**

3. A charged spherical shell of radius  $R$  has a total charge  $Q$  placed inside an uncharged conducting spherical shell that has an inner radius  $a$  and outer radius  $b$ . **Find :**
- The electric field every where, i.e. in each region 1,2,3 and 4.
  - The induced surface charge densities on the inner and outer surfaces of the uncharged conducting spherical shell.

