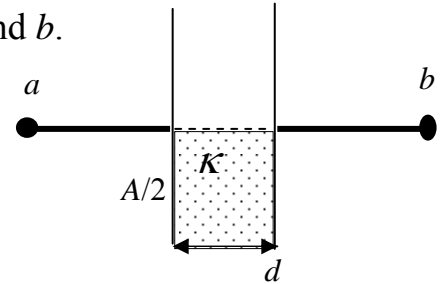


Name:..... ID#..... Section:.....

Q1 (10 points) A parallel plate capacitor of plate separation $d=1\text{mm}$ and capacitance $C_0=18\text{pF}$ is charged by a battery to charge $Q_0= 45\text{pc}$. The battery is then disconnected, and the capacitor is half- filled with dielectric of $\kappa=5$, as shown in the figure.

- Find the equivalent capacitance (C).
- Find the potential difference (V) between points a and b .
- Find the electric field (E) inside the dielectric.



Solution:

$$\text{a) } C_0 = \frac{\epsilon_0 A}{d}, C = C_1 + C_2 = \frac{\epsilon_0 (A/2) \kappa}{d} + \frac{\epsilon_0 (A/2)}{d}$$

$$C = \frac{\epsilon_0 A}{d} \cdot \frac{\kappa + 1}{2} = C_0 \frac{\kappa + 1}{2} = 54\text{pF}$$

$$\text{b) } Q_0 = Q = CV, V = 45\text{pC} / 54\text{pF} = 0.833\text{V}$$

$$\text{c) } E = V/d = 833.3\text{V/m}$$

Q2 (10 points) In the shown circuit:

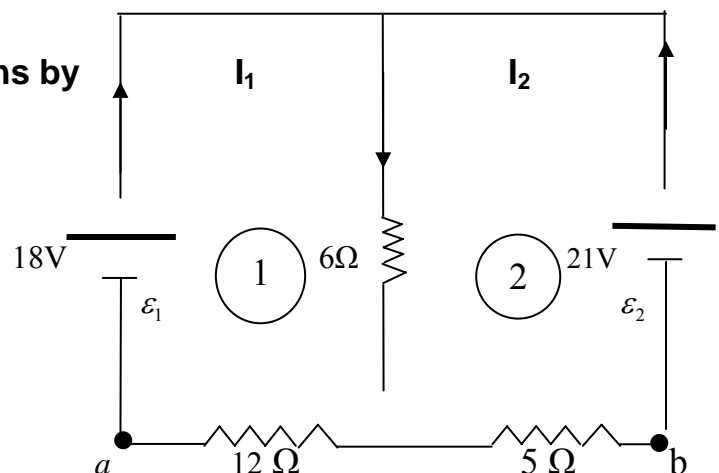
(a) Write the loop and junction equations by

I_3 applying krichhoff's rules.

(b) If $I_1 = 0.445\text{A}$, find I_2 and I_3 .

(c) What is the power output of ϵ_2 ?

(d) Find the potential between a and b .



Solution:

$$\begin{aligned} \text{a) } I_1 - I_2 + I_3 &= 0 \\ 12I_1 + 6I_2 &= 18 \\ 6I_2 + 5I_3 &= 21 \end{aligned}$$

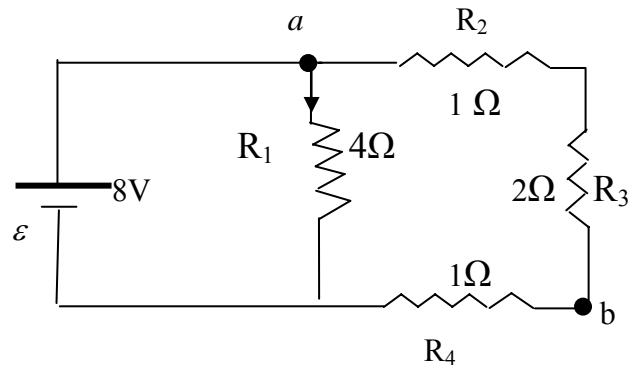
$$\text{b) } I_2 = 2.11\text{A} \quad I_3 = 1.668\text{A}$$

c) $P_{\text{out}} = \varepsilon_2 \cdot I_3 = 35.03 \text{ W}$

d) $V_{\text{ab}} = -12 I_1 + 5 I_3 = 3\text{V}$

Q3 (10 points) In the shown circuit, Find:

- (a) The equivalent resistance.
- (b) The current I_1 .
- (c) The potential difference between a and b .
- (d) The power dissipated in R_3 .



Solution:

a) $R_{\text{eq}} = \{R_1 // [R_2 = R_3 = R_4]\}$

$$= \{4//4\} = 2\Omega$$

b) $I_1 = 8/R_1 = 2\text{A}$

c) $I_2 = \frac{8}{(R_2 + R_3 + R_4)} = 2\text{A}, V_{\text{ab}} = I_2(R_2 + R_3) = 6\text{V}$

d) $P = I_2^2 \cdot R_3 = 8\text{W}$

Useful constants

$$K=9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$$

$$M_p=1.67 \times 10^{-27} \text{ kg}$$

$$\varepsilon_0 = 8.854 \times 10^{-12} \text{ C}^2 / \text{N}\cdot\text{m}^2,$$

$$e = 1.602 \times 10^{-19} \text{ C}$$

$$m_e=9.1 \times 10^{-31} \text{ kg}$$

$$g=10 \text{ m/s}^2$$